## Sixth and Seventh Regular Math

#### McElderry/Tomczyk

All work is taught and guided on the McElderry/Tomczyk Website. Watch videos and complete any practice posted on the website for each day. Complete all problems on worksheets.

https://sites.google.com/scsreading.org/scsmiddleschoolmathcybersnowda/home?a uthuser=1

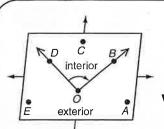
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## Day Six

# Measure and Draw Angles

Name \_\_\_\_\_

Date \_\_\_\_\_

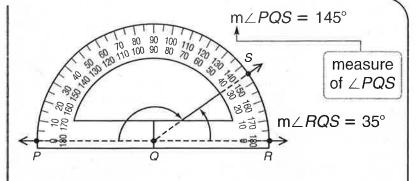


Angle:  $\angle DOB$  or  $\angle BOD$ 

or ∠*O* 

Sides:  $\overrightarrow{OD}$ ,  $\overrightarrow{OB}$ Vertex: O

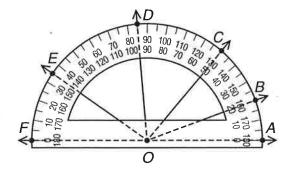
Plane EAC contains  $\angle DOB$ . Point C is in the interior of  $\angle DOB$ . Points E and A are in the exterior of  $\angle DOB$ .



Read the measure of each angle where  $\overrightarrow{QS}$  crosses the protractor.

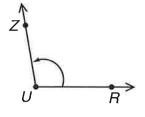
Name the points that are in the interior and the points that are in the exterior of the given angle. Then find the measure of the angle.

- 1. ∠AOE \_\_\_\_\_
- 2. ∠AOC \_\_\_\_\_
- **3.** ∠*AOD* \_\_\_\_\_
- **4.** ∠FOC \_\_\_\_\_
- **5.** ∠*FOD*

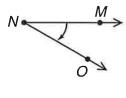


Estimate the measure of each angle. Then use a protractor to find the exact measure.

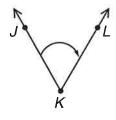
6



7.



8



Use a protractor to draw each angle.

**9.** 15°

**10.** 150°

**11.** 65°

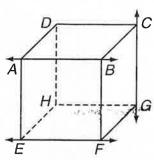
**12.** 135°

**13.** 55°

**14.** 110°

Day Six Lines and Angles

Name \_

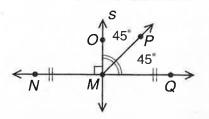


 $\overrightarrow{AB}$  and  $\overrightarrow{EF}$  are in the same plane.

 $\overrightarrow{AB}$  and  $\overrightarrow{EF}$  are parallel lines.

 $\overrightarrow{AB}$  and  $\overrightarrow{CG}$  are in different planes.

 $\overrightarrow{AB}$  and  $\overrightarrow{CG}$  are skew lines.



M is the midpoint of  $\overline{NQ}$ .

$$\overline{NM} \cong \overline{QM}$$

is congruent to

Line s is a perpendicular bisector of  $\overline{NQ}$ .  $\overrightarrow{MP}$  is the angle bisector of  $\angle OMQ$ .

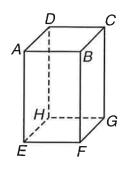
$$\angle OMP \cong \angle PMQ$$

Use the figure at the right.

1. Name a line that is parallel to the given line.

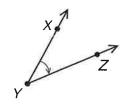
a.  $\overrightarrow{FG}$  b.  $\overrightarrow{AB}$ 

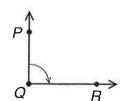
**2.** Name the lines that form a pair of skew lines with  $\overrightarrow{DC}$ .

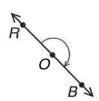


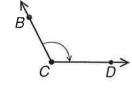
Classify each angle as right, acute, obtuse, or straight. Use a protractor to check.

3.









Write true or false. If false, explain why. Use the figure at the right.

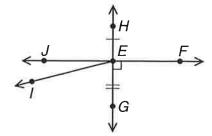
7. 
$$\overrightarrow{JF} \perp \overrightarrow{EI}$$

**8.**  $\overrightarrow{EI}$  bisects  $\angle JEG$ .

**9.** 
$$\angle JEH \cong \angle FEG$$

10. *EH* | *EF* 

**12.** *E* is the midpoint of *HG* 



Draw a figure for each description. Use a separate sheet of paper.

**13.** 
$$\angle ABC$$
 is bisected by  $\overrightarrow{BX}$ .

**15.** 
$$\overline{MN}$$
 bisects  $\overline{OP}$  at  $Y$ .

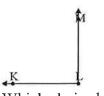
**16.** 
$$\overrightarrow{BC} \perp \overrightarrow{FG}$$

#### **Estimating Angle**

Name:

Solve each problem.

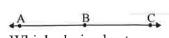
1)



Which choice best represents ∟KLM?

- A. 139°
- B. 7°
- C. 90°
- D. 44°

2)



Which choice best represents ∟ABC?

- A. 81°
- B. 16°
- C. 180°
- D. 150°

3)



Which choice best represents ∟ABC?

- A. 168°
- B. 88°
- C. 129°
- D. 39°

Answers

- •0
- 2.
- 3.
- 4. \_\_\_\_\_
- 5. \_\_\_\_\_
- 6.
- 7.
- 8.
- 9.

4)



Which choice best represents ∟ KLM?

- A. 65°
- B. 8°
- C. 138°
- D. 97°

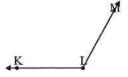
5)



Which choice best represents ∟ ABC?

- A. 34°
- B. 80°
- C. 9°
- D. 57°

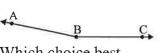
**6)** 



Which choice best represents ∟KLM?

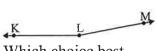
- A. 143°
- B. 119°
- C. 30°
- D. 97°

7)



- Which choice best represents LABC?
- A. 168°
- B. 115°
- C. 87°
- D. 22°

8)



Which choice best represents ∟KLM?

- A. 169°
- B. 68°
- C. 141°
- D. 47°

9)



Which choice best represents ∟KLM?

- A. 26°
- B. 117°
- C. 148°
- D. 82°

## Day Seven **Angle Pairs**

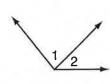
Name \_\_\_\_\_

Date =

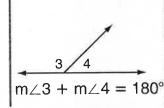
If the measures have a sum of 90°, those angles are complementary angles.

If the measures of any two angles of any two angles have a sum of 180°, those angles are supplementary angles.

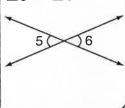
 $\angle 1$  and  $\angle 2$  are adjacent angles.



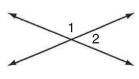
 $\angle$ 3 and  $\angle$ 4 form a linear pair.

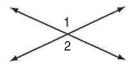


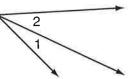
 $\angle 5$  and  $\angle 6$  are vertical angles. ∠5 ≅ ∠6

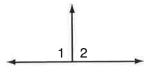


Are  $\angle 1$  and  $\angle 2$  adjacent angles? Write yes or no. If no, explain why.



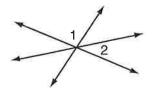


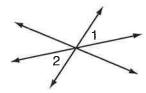


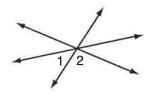


Are  $\angle 1$  and  $\angle 2$  vertical angles? Write yes or no. If no, explain why.

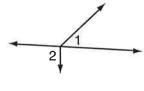
5.







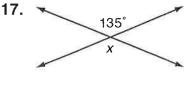
8.



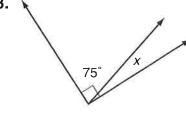
Write whether the angle pairs are complementary angles, supplementary angles, or neither.

**16.** 95°, 85°

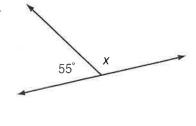
Find the value of x.



18.



19.

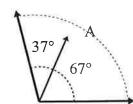


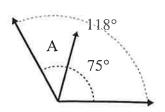
Finding Missing Angle

Name:

Determine the value of 'A'.

1)



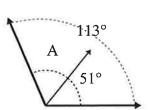


Answers

12.

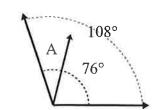
3)

5)



4)

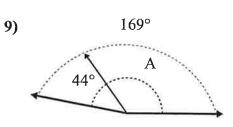
6)



136°

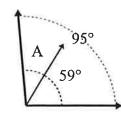
104°

7)

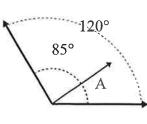


68°

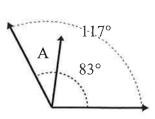
8)



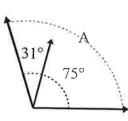
10)



11)



12)





Finding Missing Angle

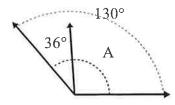
Name:

#### Determine the value of 'A'.

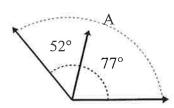
1)

3)

5)



2)

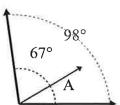


Answers

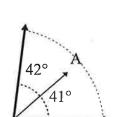
12.

100°

4)

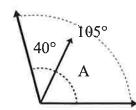


7)

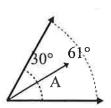


8)

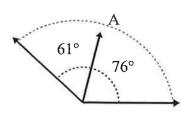
6)



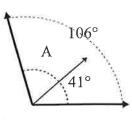
9)



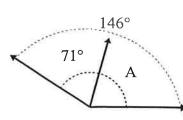
10)



11)



12)

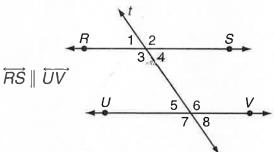


#### Day Eight Angles of Parallel Lines

Name

Date \_

A transversal intersects two or more lines at different points. Line *t* is a transversal.



A transversal forms pairs of angles with special names.

Corresponding angles:

 $\angle 1$  and  $\angle 5$ ;  $\angle 2$  and  $\angle 6$ ;  $\angle 3$  and  $\angle 7$ ;  $\angle 4$  and  $\angle 8$ 

$$\angle 1 \cong \angle 5$$
;  $\angle 2 \cong \angle 6$ ;  $\angle 3 \cong \angle 7$ ;  $\angle 4 \cong \angle 8$ 

Alternate interior angles:

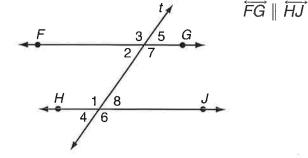
$$\angle 3$$
 and  $\angle 6$ ;  $\angle 4$  and  $\angle 5$   
 $\angle 3 \cong \angle 6$ ;  $\angle 4 \cong \angle 5$ 

Alternate exterior angles:

$$\angle 1$$
 and  $\angle 8$ ;  $\angle 2$  and  $\angle 7$   
 $\angle 1 \cong \angle 8$ ;  $\angle 2 \cong \angle 7$ 

Identify each pair of angles as alternate interior, alternate exterior, corresponding, or none of these.

- ∠1 and ∠2 \_\_\_\_\_\_
- **2.** ∠3 and ∠6 \_\_\_\_\_
- **3.** ∠2 and ∠8 \_\_\_\_\_
- **4.** ∠6 and ∠7 \_\_\_\_\_

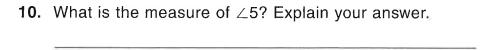


Use the figure above to find each measure.

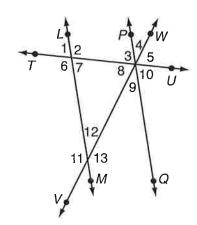
- **5.**  $m \angle 4$  when  $m \angle 2 = 45^{\circ}$  **6.**  $m \angle 7$  when  $m \angle 8 = 45^{\circ}$
- **7.**  $m \angle 3$  when  $m \angle 6 = 135^{\circ}$
- **8.**  $m \angle 1$  when  $m \angle 5 = 45^{\circ}$

**Problem Solving** In the figure at the right,  $\overrightarrow{LM} \parallel \overrightarrow{PQ}$ .  $\overrightarrow{TU}$  and  $\overrightarrow{VW}$  are transversals. Also,  $m \angle 3 = 75^{\circ}$  and  $m \angle 12 = 35^{\circ}$ . Use the figure for exercises 9-11.

**9.** What is the measure of  $\angle 8$ ? Explain your answer.

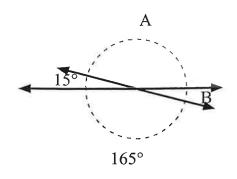


11. What is the measure of  $\angle 1$ ? Explain your answer.

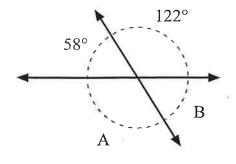


Find the value of angle 'A' and angle 'B'.

1)



2)



Answers

1.....

2.

3.6

4. \_\_\_\_\_

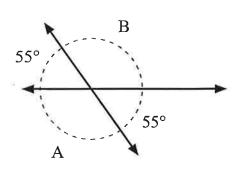
5, \_\_\_\_\_

j. ,\_\_\_\_\_

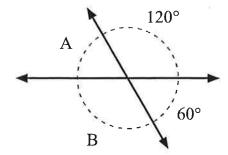
7.\_\_\_\_

8. \_\_\_\_\_

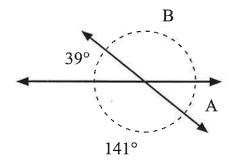
3)



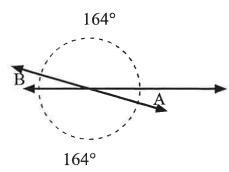
4)



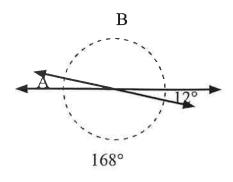
5)



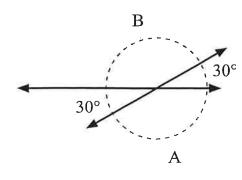
6)



7)



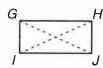
8)



Regular polygon: all sides and all angles are congruent.

Diagonal: a line segment that connects two vertices of a polygon and is not a side.

#### Convex Polygon



 $\overline{GJ}$  and  $\overline{HI}$  are diagonals. All diagonals have all points inside the polygon.

#### **Concave Polygon**



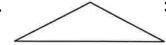
LP is a diagonal that has points outside the polygon.

Write regular or not regular for each polygon. Then write whether the polygon is convex or concave.

1.



2.



3.



4.



Draw each polygon. Write the number of sides and vertices for each.

- 5. pentagon
- 6. decagon
- 7. quadrilateral
- 8. heptagon

Find the number of diagonals for each convex polygon.

- 9. rhombus \_\_\_\_\_ 10. hexagon \_\_\_\_ 11. pentagon \_\_\_\_ 12. triangle \_\_\_\_

On a separate sheet of paper draw the polygon described. Then draw and name its diagonals.

**13.** quadrilateral *ABCD* with no right angles 14. concave pentagon MNRST

## **Angles of Polygons**

Name \_\_\_\_\_

Polygon	Number of Sides	Number of Triangles Formed by Diagonals from One Vertex	Sum of the Measures of the Interior Angles	
pentagon	5	5 - 2 = 3	$3 \times 180^{\circ} = 540^{\circ}$	
hexagon	6	6 - 2 = 4	4 × 180° = 720°	
octagon	8	8 - 2 = 6	$6 \times 180^{\circ} = 1080^{\circ}$	
<i>n</i> -gon	n	n – 2	$(n-2) \times 180^{\circ}$	

#### Find the number of triangles formed by the diagonals from one vertex of each polygon.

- **1.** 14-gon \_\_\_\_\_
- 2. rectangle \_\_\_\_\_
- **3.** 19-gon \_\_\_\_\_

- 4. nonagon \_\_\_\_\_
- **5.** 12-gon \_\_\_\_\_
- 6. parallelogram \_\_\_\_\_

Find the sum of the measures of the interior angles of each polygon.

**7.** 14-gon

8. rhombus

**9.** 19-gon

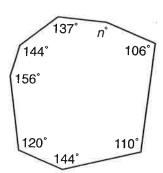
**10.** nonagon

**11.** 12-gon

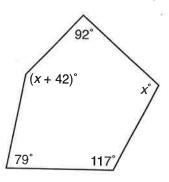
**12.** heptagon

Find the value of the variable in each polygon.

13.



14.



## Problem Solving

- 15. Derek draws a polygon. The sum of its 16. Four of the interior angles of Fiona's interior angles is 1440°. What kind of polygon does Derek draw?
  - hexagon measure 167°, 105°, 145°, and 135°. The other interior angles are congruent to each other. What are the measures of the other angles?

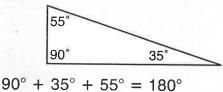
The straight of the straight o

## **Angles of Triangles** and Quadrilaterals

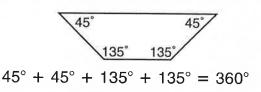
Name \_\_\_\_\_

Date

The sum of the measures of the interior angles of a triangle is 180°.

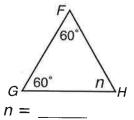


The sum of the measures of the interior angles of a quadrilateral is 360°.

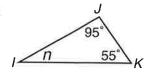


Find the measure of the third angle of each triangle.

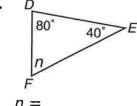
1.



2.



$$n =$$



**4.** 
$$\angle K = 38^{\circ}, \angle L = 89^{\circ}, \angle M =$$
\_\_\_\_\_

**5.** 
$$\angle X = 85^{\circ}, \angle Y = 49^{\circ}, \angle Z =$$

Find the measure of the fourth angle of each quadrilateral.

**6.** 
$$\angle E = 99^{\circ}$$
,  $\angle F = 47^{\circ}$ , **7.**  $\angle J = 23^{\circ}$ ,  $\angle K = 109^{\circ}$ , **8.**  $\angle Q = 88^{\circ}$ ,  $\angle R = 93^{\circ}$ ,  $\angle G = 79^{\circ}$ ,  $\angle H =$   $\angle L = 97^{\circ}$ ,  $\angle M =$   $\angle S = 97^{\circ}$ ,  $\angle T =$ 

7. 
$$\angle J = 23^{\circ}, \angle K = 109^{\circ},$$
  
 $\angle I = 97^{\circ} \angle M =$ 

**7.** 
$$\angle J = 23^{\circ}, \ \angle K = 109^{\circ},$$
 **8.**  $\angle Q = 88^{\circ}, \ \angle R = 93^{\circ},$   $\angle L = 97^{\circ}, \ \angle M = \underline{\hspace{1cm}}$   $\angle S = 97^{\circ}, \ \angle T = \underline{\hspace{1cm}}$ 

Find the value of n in each quadrilateral.

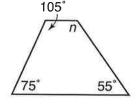
9.



10.

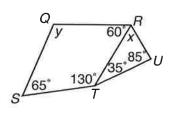


11.

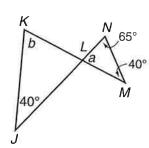


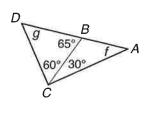
Find the value of each variable.

12.



13.





## Problem Solving

15. Trapezoid EFGH has two pairs of congruent angles. One of the angles measures 124°. What are the measures of the other angles?

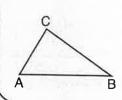
## Day Ten Triangles

Name \_\_\_\_\_

Date \_\_\_\_\_

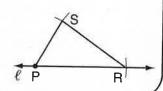
Construct  $\triangle PRS$  congruent to  $\triangle ABC$ .

- Draw  $\overline{PR} \cong \overline{AB}$  on line  $\ell$ .
- Measure AC. From point P construct an arc. Measure BC.
   From point R construct an arc.
- Label point S. Draw  $\overline{PS}$  and  $\overline{RS}$ .  $\triangle PRS \cong \triangle ABC$



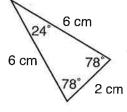




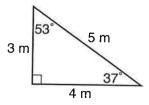


Classify each triangle by the measure of its sides and by the measure of its angles.

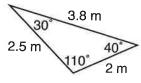
1.



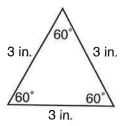
2.



3.



4.



Use a protractor and a centimeter ruler to measure the sides and angles of each triangle. Then classify the triangle by its sides and angles.

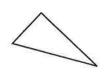
5.



6.



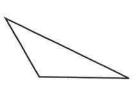
7.



8.



9



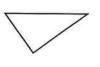
10.



11.



12.



Draw the triangle indicated. Then construct a triangle congruent to it.

**13.** scalene  $\triangle RST$ 

**14.** acute △*CDE* 

**15.** isosceles △*OPQ* 



Name \_\_\_\_\_\_
Date

l'	quadrilateral	
trapezoid		parallelogram
	rectangle	rhombus
		square

Construct parallelogram MNOP.

- 1. Draw  $\overline{MN}$  and  $\overline{MP}$ .
- 2. From P and N, construct arcs.
- 3. Label <u>O.</u> Draw <u>NO</u> and <del>OP</del>.



MNOP is a parallelogram.

 $\begin{array}{c|c}
\hline
1 & B \\
\hline
M & N \\
\hline
3 & P \\
\hline
M & N
\end{array}$ 

Complete the table. Write yes or no for each description.

	Description	Rhombus	Square	Rectangle	Parallelogram	Trapezoid
1,	4 right angles					
2.	opposite sides parallel					
3.	all sides congruent					

Write whether each statement is true or false. Explain.

- **4.** Some rectangles are trapezoids.
- 5. All rectangles are parallelograms.
- **6.** Some parallelograms are rectangles.
- 7. All rhombuses are squares.

Construct the figure described.

8. parallelogram ABCD

9. rhombus RSTU with each side 2 cm long

Point M is the center of circle M.

MA is a radius.

AN is a diameter.

AC is a chord.

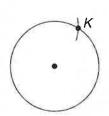
∠AMC is a central angle.

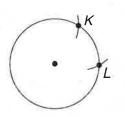
ACN is a semicircle,  $m\widehat{ACN} = 180^{\circ}$ 

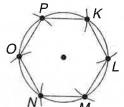
 $\widehat{ABC}$  is a minor arc.  $\widehat{mABC}$  < 180°

 $\widehat{CON}$  is a major arc. m $\widehat{CON} > 180^{\circ}$ 

Construct a regular hexagon by using a circle.







KLMNOP is a regular hexagon.

Use a compass to construct a circle with a radius of 2 cm. Then draw and label each of the following:

- 1. center: point O
- 2. radius: OR
- **3.** central angle:  $\angle ROT$  **4.** diameter:  $\overline{XY}$

**5.** chord:  $\overline{RS}$ 

**6.** chord:  $\overline{YZ}$ 

Use circle M in the display above for exercises 7–9.

- 7. Name one semicircle other than  $\widehat{ACN}$ :
- 8. Name one minor arc other than  $\widehat{ABC}$ :
- **9.** Name one major arc other than  $\widehat{CON}$ :

For each statement, write always, sometimes, or never.

- **10.** One endpoint of every radius of a circle is the center of the circle.
- 11. Chords pass through the center of a circle.
- 12. A diameter forms a straight angle.
- 13. A central angle of a circle has its vertex on the circle.

Construct each regular polygon by using a circle. Explain your process.

- 14. an octagon
- **15.** a hexagon

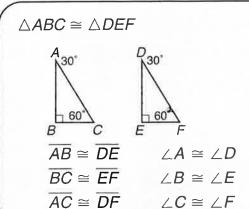
**16.** a nonagon

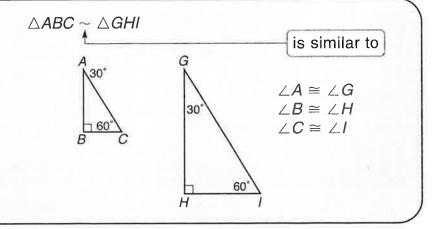
Day Eleven

## Congruent and Similar Polygons

Name \_\_\_\_

Date :





Do the polygons appear to be congruent, similar, or neither?

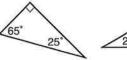








3.





4.

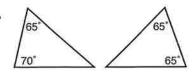


5.



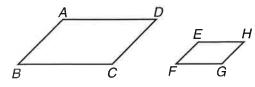


6.

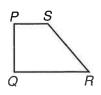


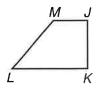
#### Name the corresponding congruent parts.

Parallelogram ABCD ~ Parallelogram EFGH



Trapezoid *PQRS* ≅ Trapezoid *JKLM* 





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#### Problem Solving

**17.** In the figures at the right,  $KLMN \cong WXYZ$ . Find the measure of  $\angle Y$  and  $\angle W$ and the lengths of XY and WX.

